

# ALMA Capturing

How does  
the Atacama Large Millimeter Array telescope  
capture photons?

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Dreamlab Technologies

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# Introduction

## 1/ Introduction

- Collaboration
- Geolocation
- Electrolocation
- Pipeline

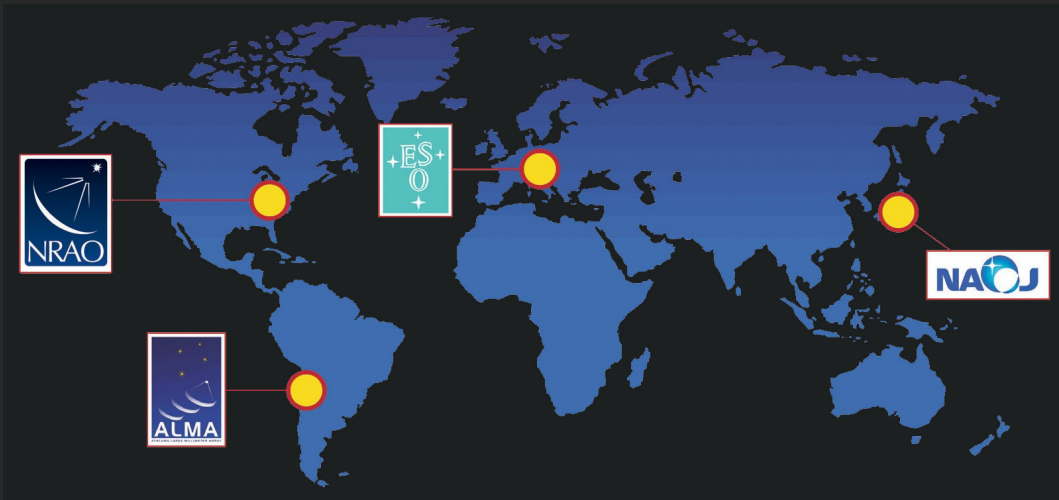
## 2/ Example

## 3/ Detail

## 4/ Conclusion



# Collaboration



# Geolocation



# Geolocation



# Geolocation



# Geolocation



1. Safety
2. Altitude
3. Humidity
4. Latitude
5. Turbulences
6. Accessibility

---

Altitude	5000m
Antenna	66
Wavelength	1mm
Frequency	300GHz
Water (WVP)	1mm
Temperature	-269°C

---



# Geolocation

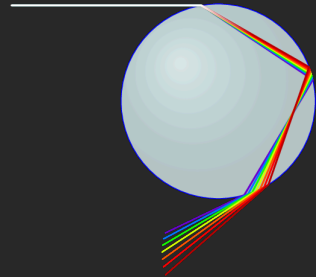


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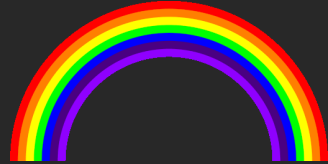
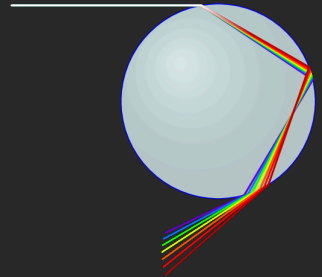


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# Geolocation

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2. Altitude
3. Humidity
4. Latitude

## Takeaway

Water + Light = Rainbow



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# Geolocation

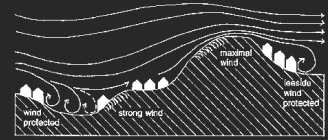


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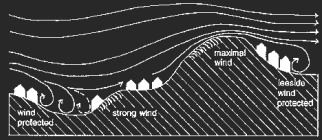
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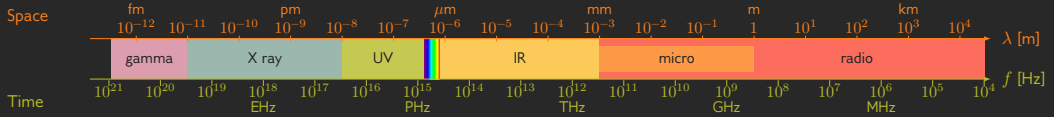


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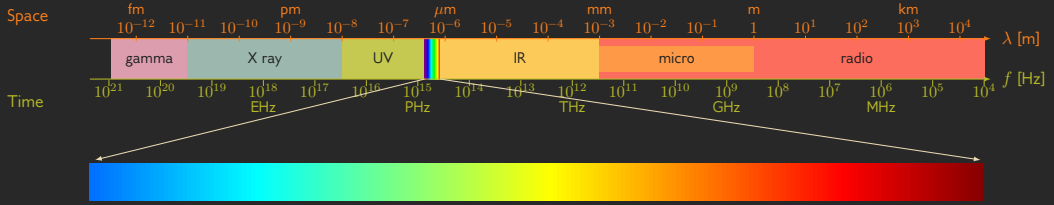
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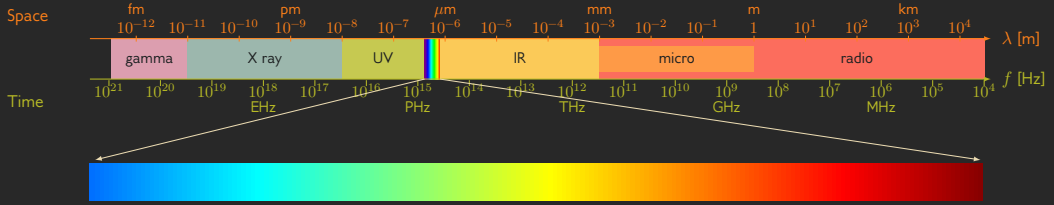
# Electrolocation



# Electrolocation



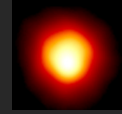
# Electrolocation



Sirius



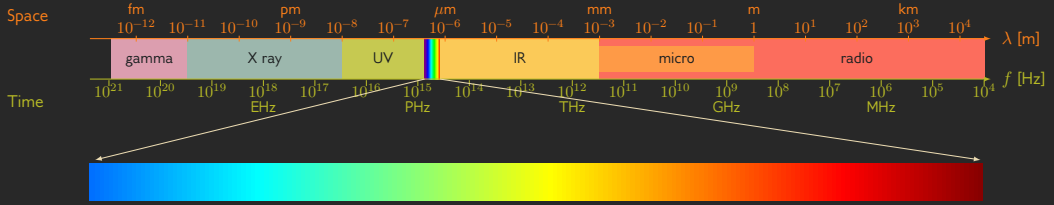
Sun



Betelgeuse



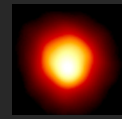
# Electrolocation



Sirius



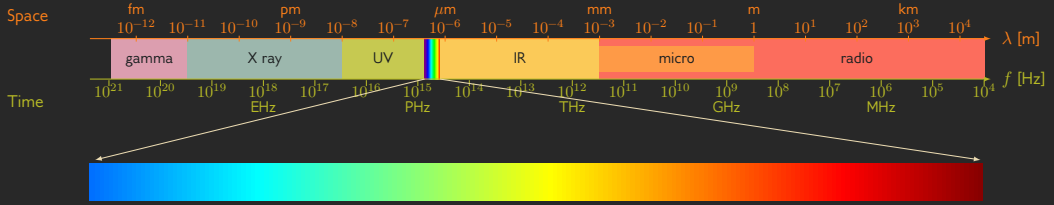
Sun



Betelgeuse

Look at the stars  
 Look how they shine for you  
 And everything you do  
 Yeah, they were all yellow

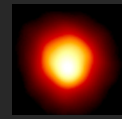
# Electrolocation



Sirius



Sun

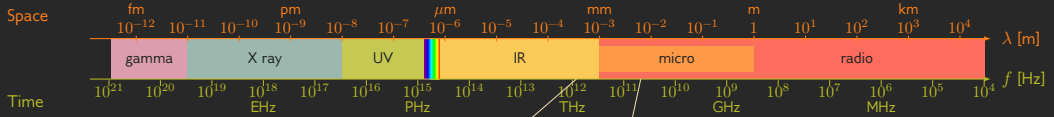


Betelgeuse

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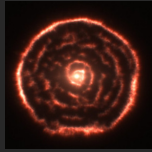
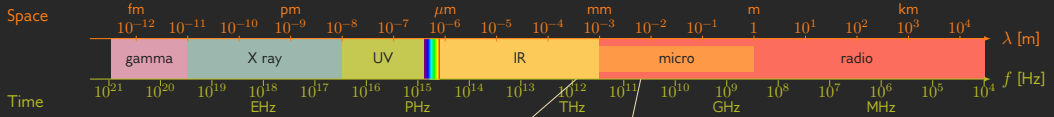
Your eye evolved to see the sun  
 Stars have different colors

# Electrolocation



ALMA (telescope)

# Electrolocation

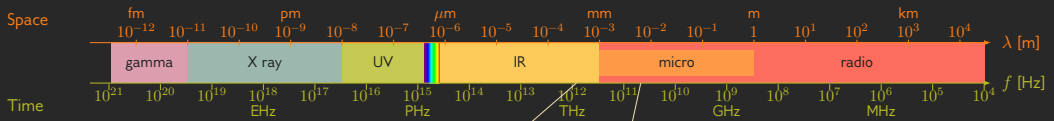


R Sculptoris (star)



ALMA (telescope)

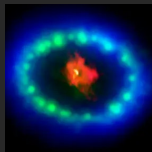
# Electrolocation



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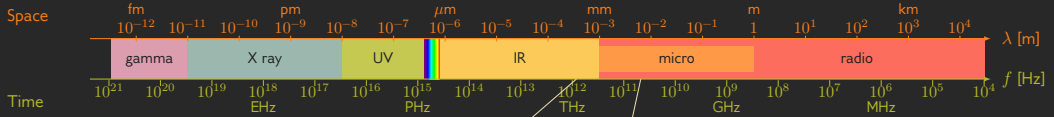


ALMA (telescope)



Sn1987a (star)

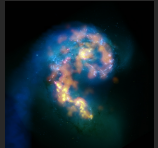
# Electrolocation



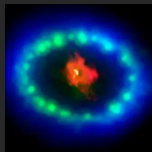
R Sculptoris (star)



ALMA (telescope)

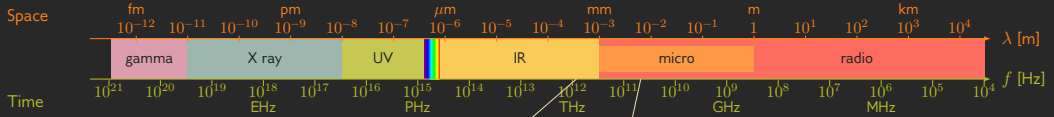


Ngc 4038/4039 (galaxy)



Sn1987a (star)

# Electrolocation



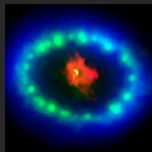
R Sculptoris (star)



ALMA (telescope)



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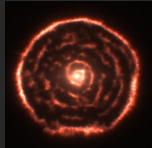
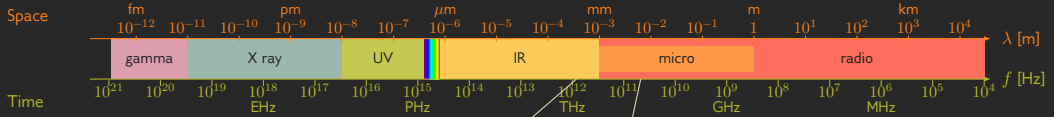


Sn1987a (star)



Hercules a (galaxy)

# Electrolocation



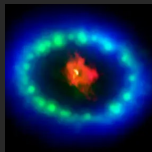
R Sculptoris (star)



ALMA (telescope)



Ngc 4038/4039 (galaxy)



Sn1987a (star)



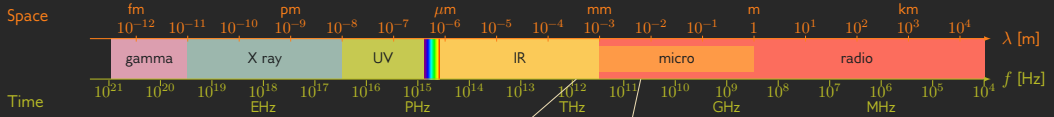
M87\* (black hole)



Hercules a (galaxy)

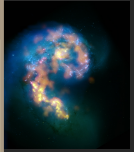


# Electrolocation



## Takeaway

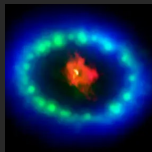
ALMA is capturing **millimeter** wavelength  
 (or **300 GHz** = 300,000,000[m/s] / 0.001[m])



K Sculptoris (star)

ALMA (telescope)

ngc 4038/4039 (galaxy)



Sn1987a (star)



M87\* (black hole)



Hercules a (galaxy)

# Pipeline

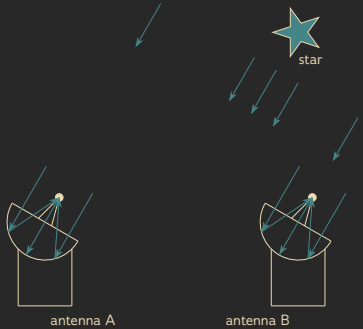


## The radio waves is ...

- — • Emited by the source

# Pipeline

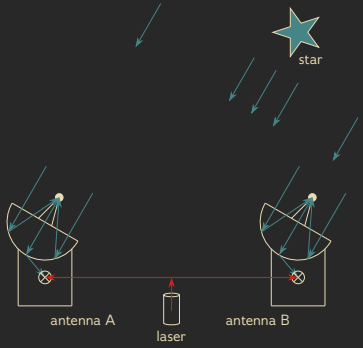
## The radio waves is ...



- — ● Emited by the source
- — ● Concentrated by the antenna  
convex reflector

# Pipeline

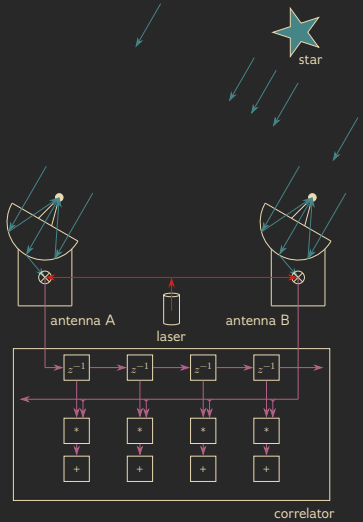
## The radio waves is ...



- Emited by the source
- Concentrated by the antenna convex reflector
- Downconverted and digitalised by mixing with the central laser frequency

# Pipeline

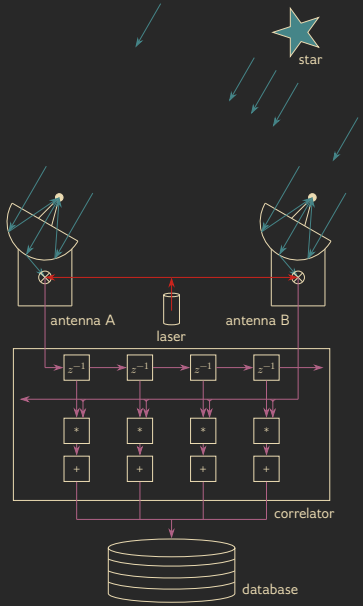
## The radio waves is ...



- — ● Emited by the source
  
- — ● Concentrated by the antenna  
convex reflector
  
- — ● Downconverted and  
digitalised by mixing with the  
central laser frequency
  
- — ● Correlated to other antenna mea-  
surement

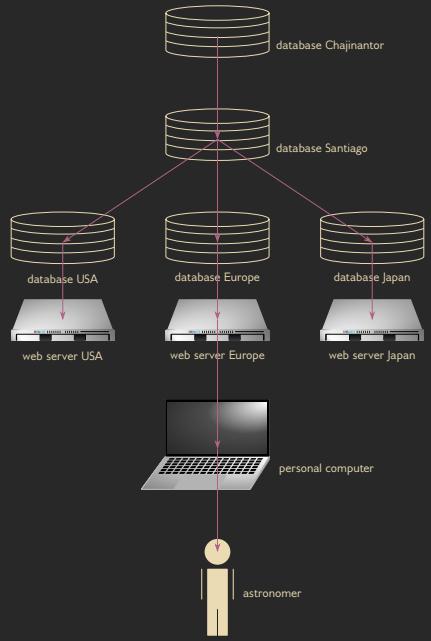
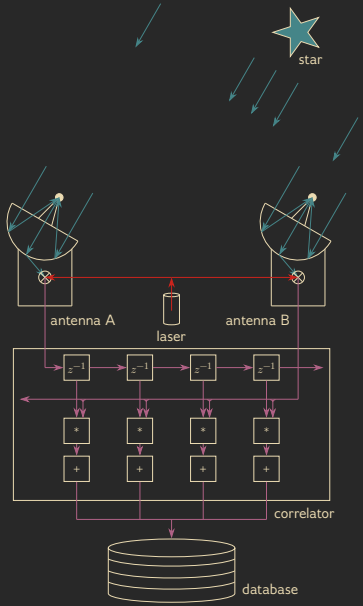
# Pipeline

## The radio waves is ...



- — ● Emited by the source
- — ● Concentrated by the antenna convex reflector
- — ● Downconverted and digitalised by mixing with the central laser frequency
- — ● Correlated to other antenna measurement
- — ● Stored in a digital database

# Pipeline



## 2/ Example

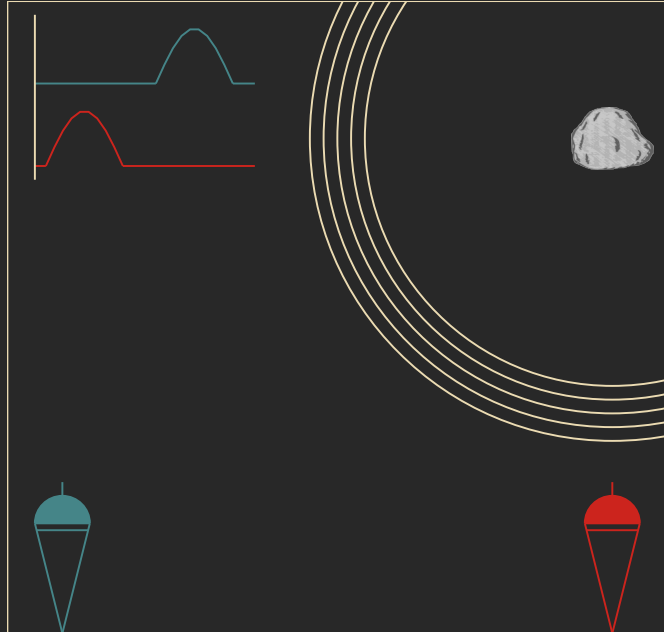
1/ Introduction

2/ Example

- Emission
- Propagation
- Reception
- Degeneration

3/ Detail

4/ Conclusion

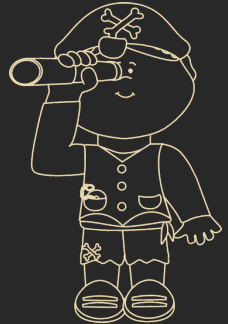




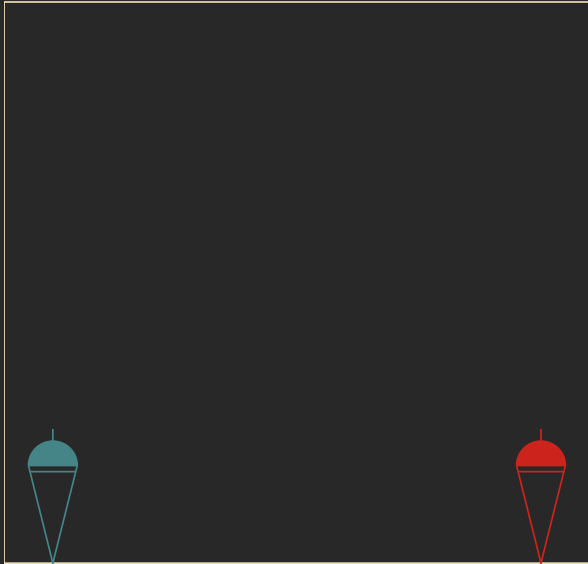




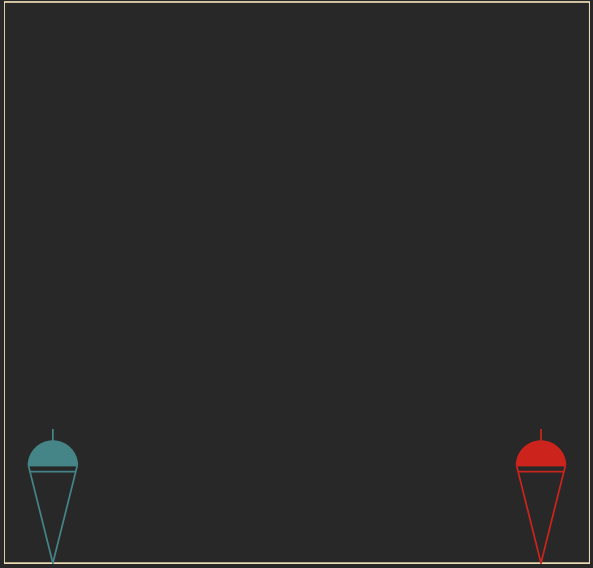
# Emission



# Emission



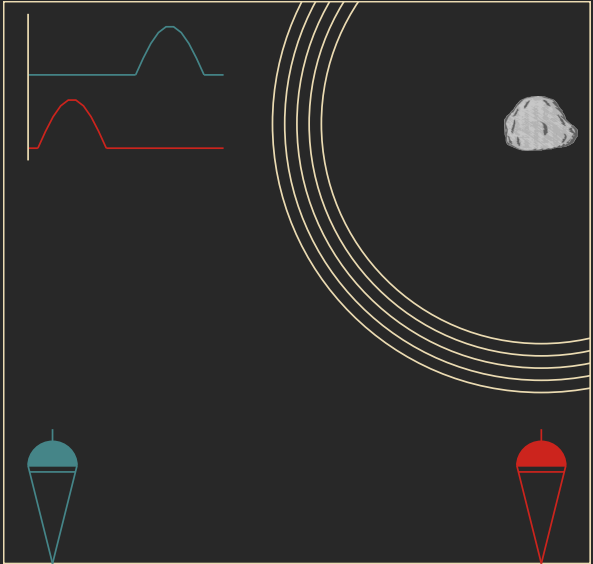
# Emission



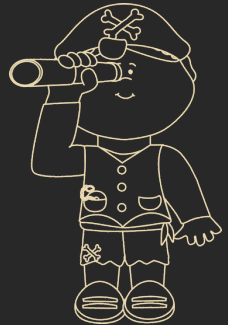
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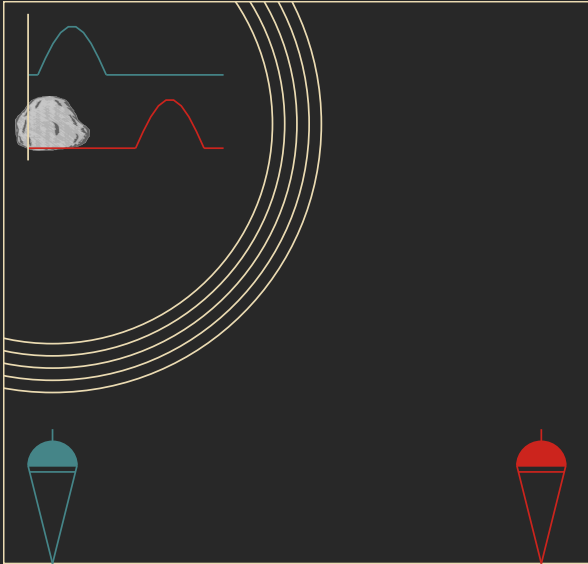


# Propragation



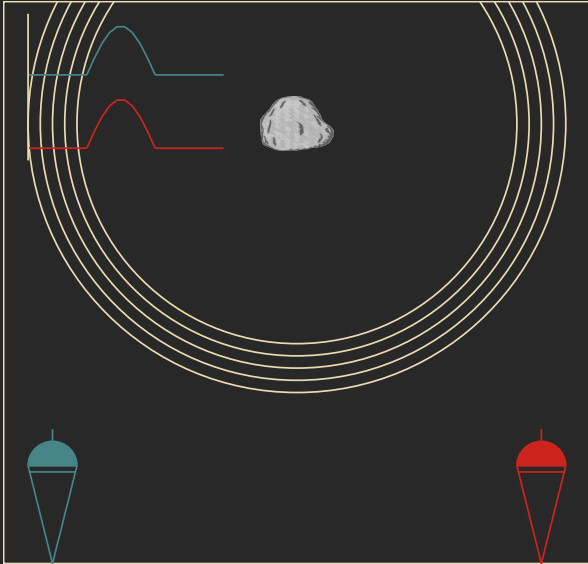


# Reception

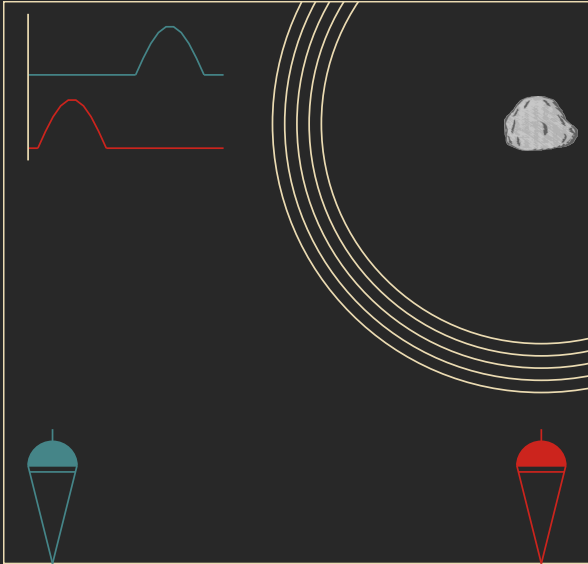


Credit: Joseph Fourier 1822

# Reception



# Reception



Credit: Joseph Fourier 1822

# Reception

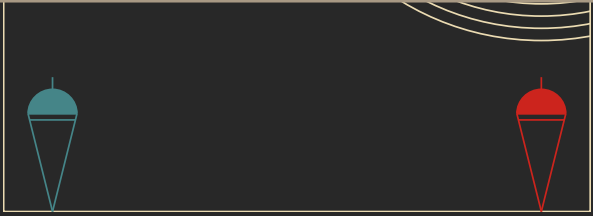


## Takeaway

The right float moves before the left one

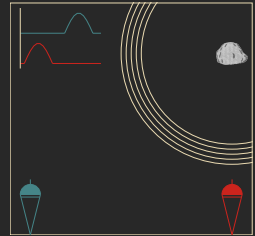
$\Leftarrow \Rightarrow$

Pedro threw the stone to the right



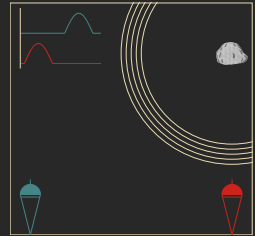
# Degeneration

The complex reality:



# Degeneration

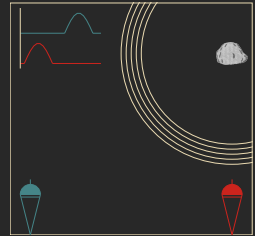
The complex reality:



Problem	Solution

# Degeneration

The complex reality:



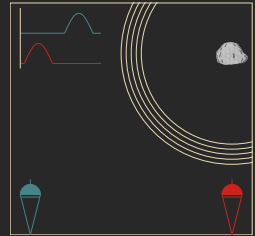
Problem	Solution
Waves are <b>continuous</b>	

Glossary: baseline = pair of detector

For n detectors, there are  $\frac{n(n-1)}{2}$  baselines

# Degeneration

The complex reality:



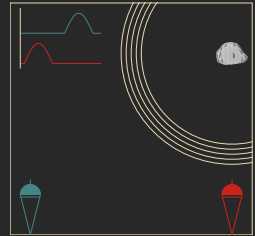
Problem	Solution
Waves are <b>continuous</b>	Have more <b>baselines</b>

Glossary: baseline = pair of detector  
 For n detectors, there are  $\frac{n(n-1)}{2}$  baselines



# Degeneration

The complex reality:



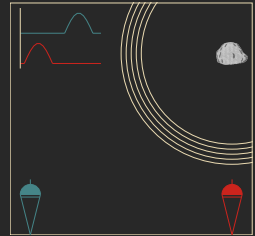
Problem	Solution
Waves are <b>continuous</b>	Have more <b>baselines</b>
Space angle have 2 <b>dimensions</b> ( $\theta$ and $\phi$ )	

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# Degeneration

The complex reality:



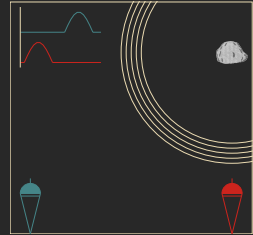
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# Degeneration

The complex reality:



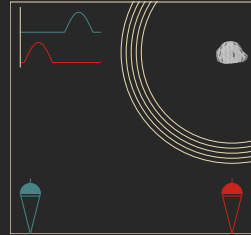
Problem	Solution
Waves are <b>continuous</b>	Have more <b>baselines</b>
Space angle have 2 <b>dimensions</b> ( $\theta$ and $\phi$ )	Have more <b>baselines</b>
There may be more than <b>one punctual</b> rock	

Glossary: baseline = pair of detector

For  $n$  detectors, there are  $\frac{n(n-1)}{2}$  baselines

# Degeneration

The complex reality:



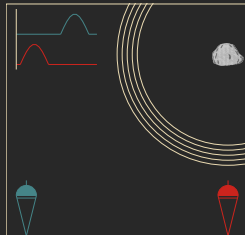
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Glossary: baseline = pair of detector

For  $n$  detectors, there are  $\frac{n(n-1)}{2}$  baselines

# Degeneration

The complex reality:



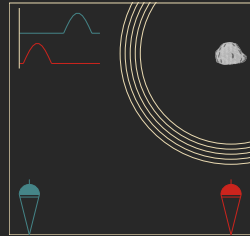
Problem	Solution
Waves are <b>continuous</b>	Have more <b>baselines</b>
Space angle have 2 <b>dimensions</b> ( $\theta$ and $\phi$ )	Have more <b>baselines</b>
There may be more than <b>one punctual</b> rock	Have more <b>baselines</b>
Electric <b>noise</b> , atmospheric <b>cloud</b> , spurious <b>signal</b>	

Glossary: baseline = pair of detector

For n detectors, there are  $\frac{n(n-1)}{2}$  baselines

# Degeneration

The complex reality:



Problem	Solution
Waves are <b>continuous</b>	Have more <b>baselines</b>
Space angle have 2 <b>dimensions</b> ( $\theta$ and $\phi$ )	Have more <b>baselines</b>
There may be more than <b>one punctual</b> rock	Have more <b>baselines</b>
Electric <b>noise</b> , atmospheric <b>cloud</b> , spurious <b>signal</b>	Calibrate, drop

Glossary: baseline = pair of detector

For  $n$  detectors, there are  $\frac{n(n-1)}{2}$  baselines

# 3/ Detail

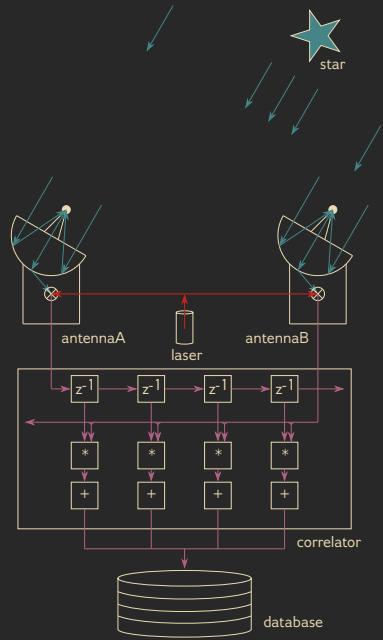
1/ Introduction

2/ Example

3/ Detail

- Antenna
- Electronic
- Correlator
- Quantity

4/ Conclusion



# Draw me a Photon!



# Electromagnetic Equation

- |    |                   |   |         |           |
|----|-------------------|---|---------|-----------|
| 1. | $\nabla \cdot E$  | $= \rho / \epsilon_0$                   | Gauss   | Flux      |
| 2. | $\nabla \cdot B$  | $= 0$                                   | Colomb  | Magnetism |
| 3. | $\nabla \times E$ | $= -\partial_t B$                       | Faraday | Induction |
| 4. | $\nabla \times B$ | $= \mu_0 (J + \epsilon_0 \partial_t E)$ | Ampere  | Circuital |

$$\partial_t^2 E = c_0^2 \nabla^2 E$$

$$\frac{\partial^2 E}{\partial t^2} = c_0^2 \left( \frac{\partial^2 E}{\partial x^2} + \frac{\partial^2 E}{\partial y^2} + \frac{\partial^2 E}{\partial z^2} \right)$$

# Hydrodynamic Equation

- |    |                   |                              |        |                   |
|----|-------------------|------------------------------|--------|-------------------|
| 1. | $\nabla \cdot V$  | $= q$                        | Fluid  | Incompressibility |
| 2. | $\nabla \cdot W$  | $= 0$                        | Vortex | Divergence        |
| 3. | $\nabla \times V$ | $= -\partial_t W$            | Vortex | Velocity          |
| 4. | $\nabla \times W$ | $= (J + \partial_t V)/a_0^2$ | Mass   | Conservation      |

$$\partial_t^2 V = a_0^2 \nabla^2 V$$

$$\frac{\partial^2 V}{\partial t^2} = c_0^2 \left( \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} \right)$$

# Electromagnetic Wave

**Photons** are the carriers of the **electric** force.

1. Created by decelerated **charges**
2. Displaced by electromagnetic field **currents**
3. Destroyed by accelerating **charges**

Without **electric** force there would be no **light** (and reciprocally)

# Electromagnetic Wave

**Photons** are the carriers of the **electric** force.

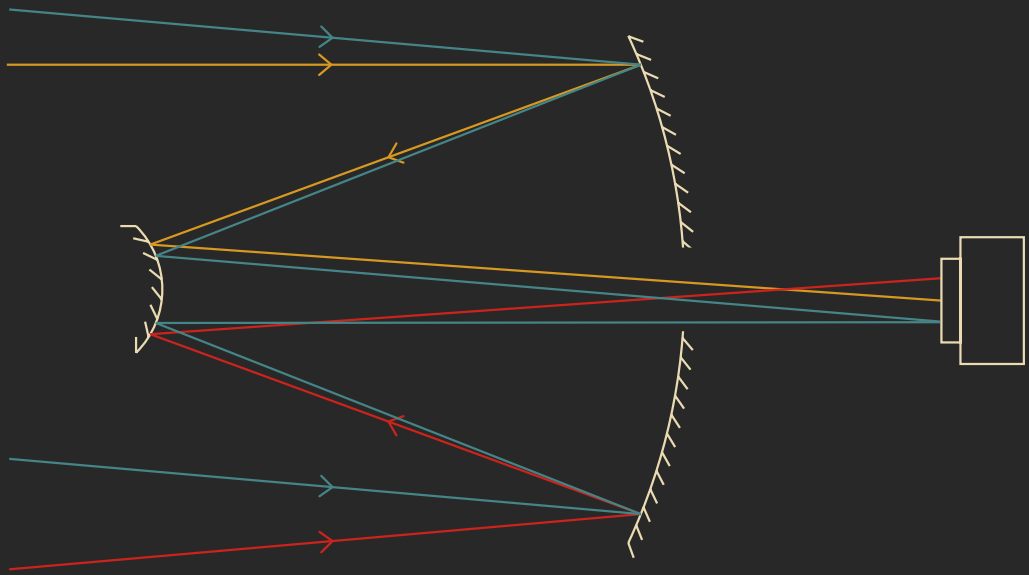
## Takeaway

2. Distortion of the electromagnetic field

3. Destroyed by accelerating **charges**

Without **electric** force there would be no **light** (and reciprocally)

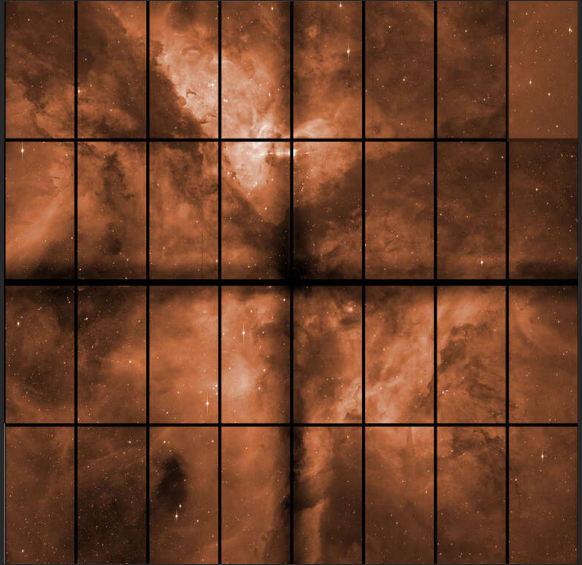
# Photon Concentration Fields



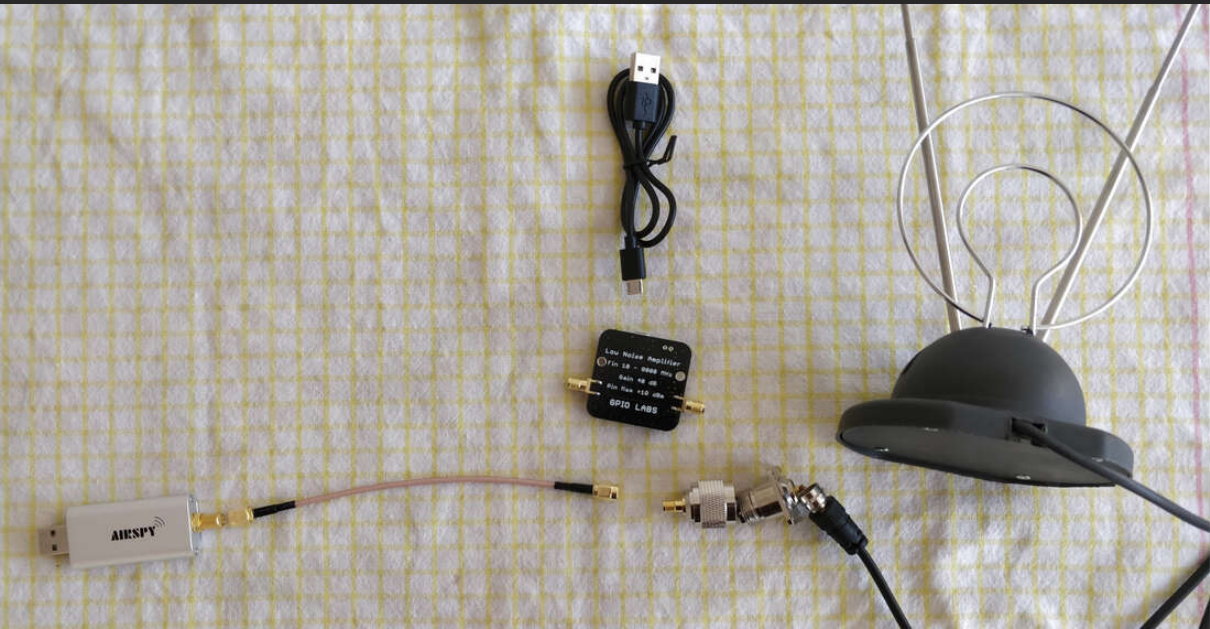
# Capturing Visible Photon with Charge-Coupled Device (CCD)



# Capturing Visible Photon with Charge-Coupled Device (CCD)



# Capturing Radio Photon: Open Wire

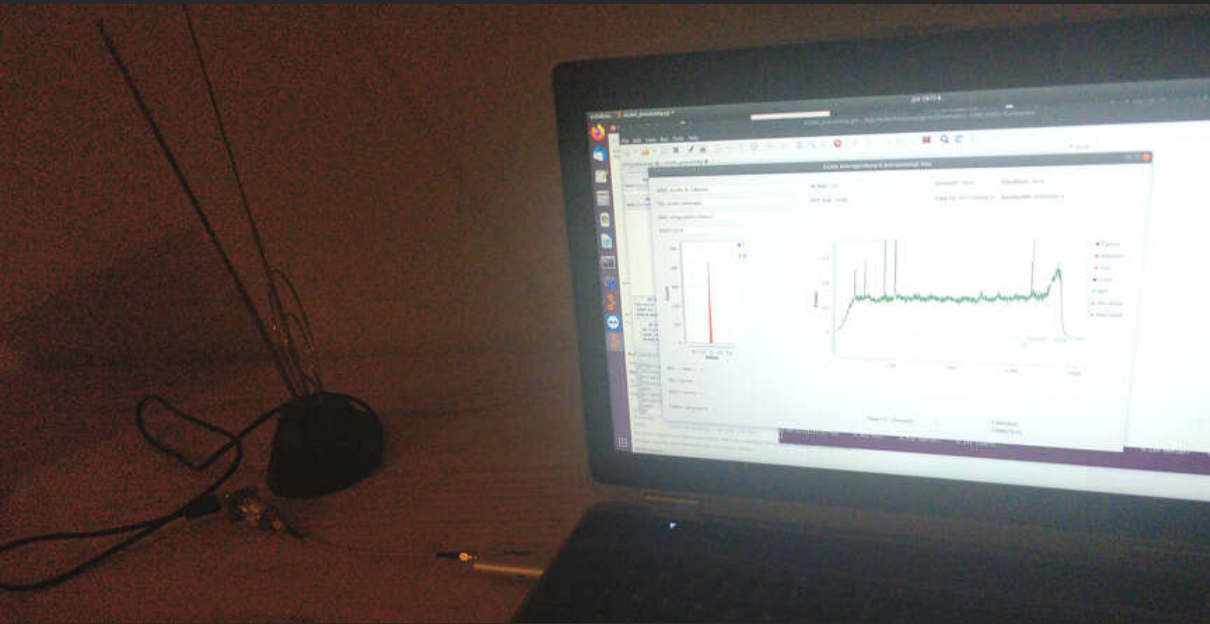




# Capturing Radio Photon: Open Wire

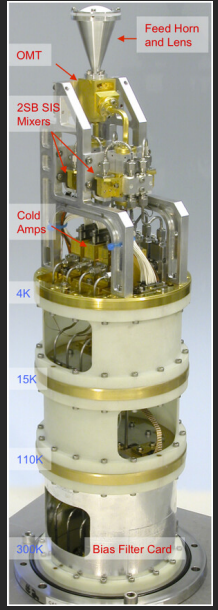
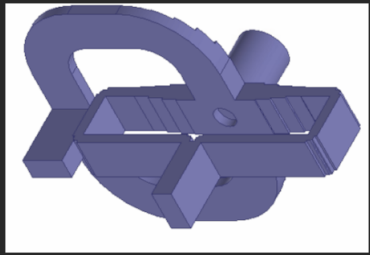
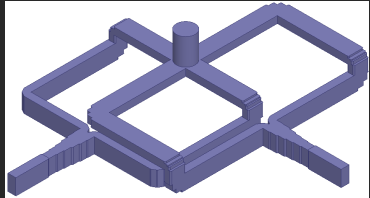
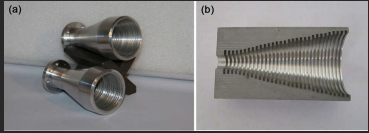


# Capturing Radio Photon: Open Wire

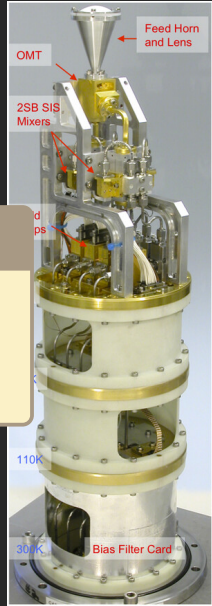
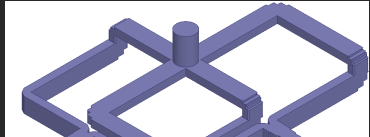
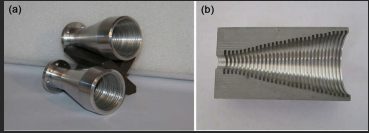


# Capturing Radio Photon: Wave Trap

# Capturing Radio Photon: Feed Horn and OMT

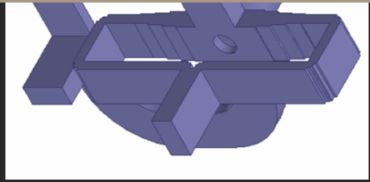
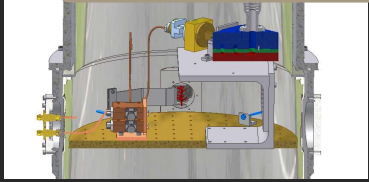


# Capturing Radio Photon: Feed Horn and OMT



## Takeaway

1. Radio antennas measure both the **amplitude AND phase** of the incident light ("coherent detectors")
2. ALMA antenna receivers have only **one pixel**



# Electronic Pipeline

From 300GHz analog to 150MHz digital



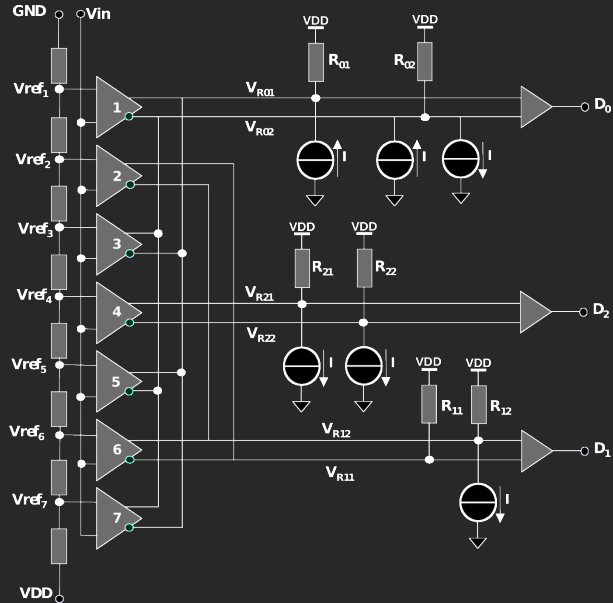
Credit: ALMA, Sergio Otarola

# Electronic Pipeline

From 300GHz analog to 150MHz digital

N	Fct	Acc	Name
1	Polarisation	OMT	OrthoMode Transducer
2	Amplification	CLNA	Cryogenic Low-Noise Amplifiers
3	Filtering	BPF	BandPass Filter
4	Equalisation	GE	Dual Gain Equalizer
5	Down-conversion	SIS	Superconductor-Insulator-Superconductor Mixer
6	Digitalization	ADC	Analog to Digital Converter
7	Multiplexing	MUX	Multiplexer
8	Transport	FO	Fiber Optic

# Digitalisation





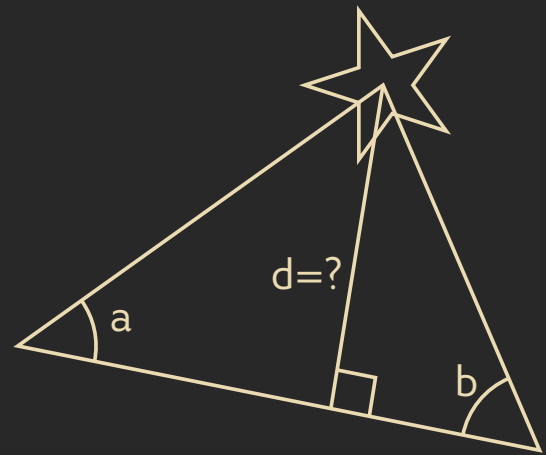
# Correlator Misunderstanding

What correlation is not:

# Correlator Misunderstanding

What correlation is not:

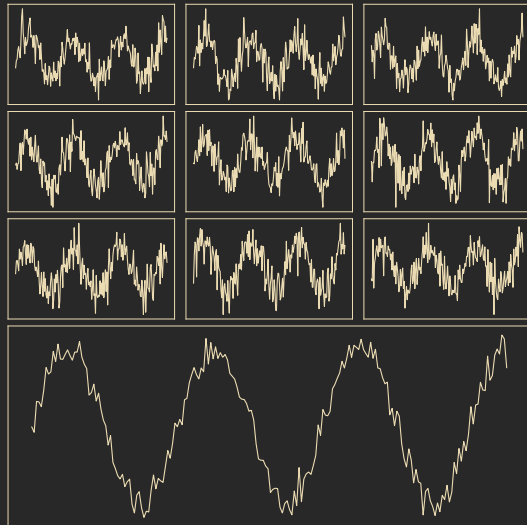
- Triangulation



# Correlator Misunderstanding

What correlation is not:

- Triangulation
- Combination

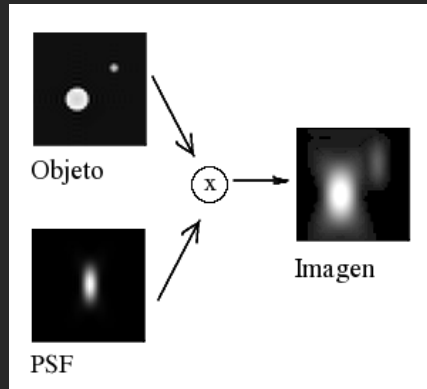


# Correlator Misunderstanding

What correlation is not:

- Triangulation
- Combination
- Convolution

$$(f * g)(x) := \int f(\tau)g(x - \tau) d\tau$$



# Correlator Misunderstanding

$$(f * g)(x) := \int f(\tau)g(x - \tau) d\tau$$

What correlation is not:

- Triangulation
- Combination
- Convolution

What correlation is:

# Correlator Misunderstanding

What correlation is not:

- Triangulation
- Combination
- Convolution

What correlation is:

- Sliding product

$$(f * g)(x) := \int f(\tau)g(x - \tau) d\tau$$

$$(f \star g)(x) := \int f^*(\tau)g(x + \tau) d\tau$$

# Correlator Misunderstanding

$$(f * g)(x) := \int f(\tau)g(x - \tau) d\tau$$

What correlation is not:

• **Takeaway**

• **The Cross-Co-Re-Lation**

• Convolution

$$)g(x + \tau) d\tau$$

What correlation is:

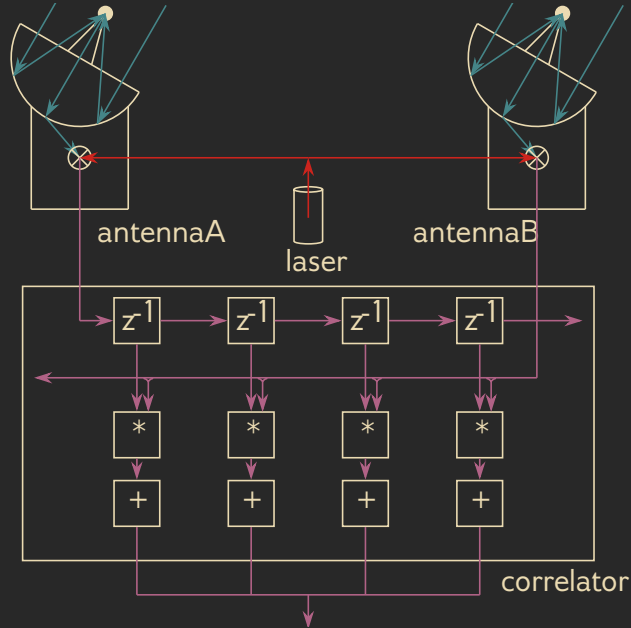
• Sliding product

# Correlator Sliding Product



# Correlator Sliding Product

# Correlator Electronics



# Quantity: Requirements

$$1.7 \times 10^{16} Hz$$

Number	Quantity	Explanation
$64^2$	Antenna Pairs	Ordered for leads vs lags
$2^2$	Cross Polarisations	XX, XY, YX, YY
8	Base Bands	Tunable from 31.25 MHz to 2 GHz
8192	Spectral Channels	Covering each baseband
62.5 MHz	Input Frequency	Digital signal speed
2	Nyquist Sampling	2 measures per wavelength

Note: Each operation is a 2 bits complex multiply-and-add.

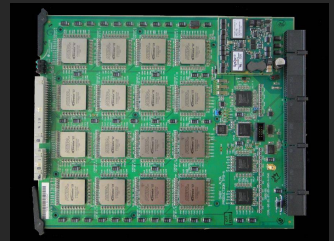
# Quantity: Processing Power

$$1.7 \times 10^{16} Hz$$

Number	Quantity	Explanation
4	Quadrants	Cupboards each processing 2 basebands
32	Planes	Shelves Filled with motherboards
4	Circuit Cards	Actually implemented with 16 cards of 16 ASICS
64	ASIC	FPGA
4096	Multiply-add	Also include including 20 bits of integration
125 MHz	Clock Rate	Real Time Electronics

Note: Each operation is a 2 bits complex multiply-and-add.

# Quantity: The Correlator Room



# 4/ Conclusion

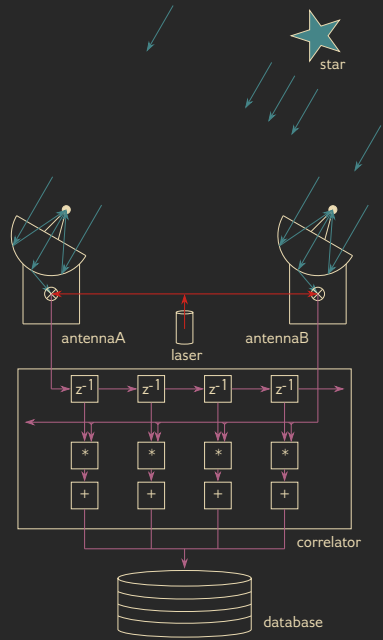
1/ Introduction

2/ Example

3/ Detail

4/ Conclusion

- Summary
- Takeaway
- Further
- Questions?



# Summary

## 1/ Introduction

- Collaboration
- Geolocation
- Electrolocation
- Pipeline

## 2/ Example

- Emission
- Propagation
- Reception
- Degeneration

## 3/ Detail

- Antenna
- Electronic
- Correlator
- Quantity

## 4/ Conclusion

- Summary
- Takeaway
- Further
- Questions?

# Takeaway

## 1 / Introduction

1. Water + light = rainbow
2. Wind + obstacle = turbulences
3. Alma captures **millimeter** wavelength

## 2/ Example

1. Rock at right  $\Leftrightarrow$  right float moves first
2. Baseline number  $>$  antenna size
3. Constrain possible scenarios with independent measures

## 3/ Detail

1. Light = wave of electromagnetic field disruption
2. Coherent detectors, measure phase **and** amplitude
3. Alma's antennas have only one pixel

## 4/ Conclusion

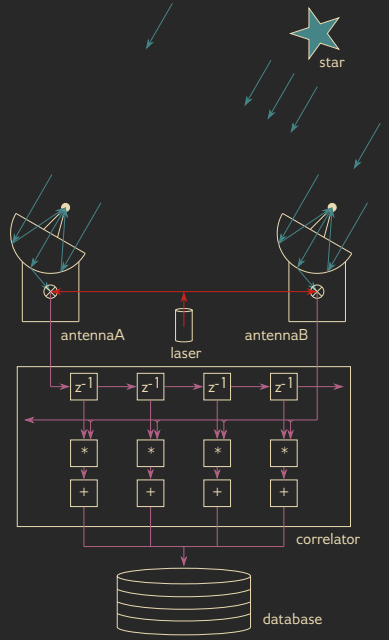
1. Physics: Electro-magnetic waves
2. Electronics: Transistors
3. Computing: Cross-correlation



# Further

ALMA	Electronics	Physics
technical handbook	digital x-correlation (gary)	aperture synthesis (me)
system diagram	transistor amplifier (utube)	spectral lines (sransom)
2030 physics (memo 621)	mixers (liam)	molecules (ddallaca)
2030 system	adc (memo 532)	radiative processes
brochure	2030 corr (memo 617)	interferometry and synthesis
manual en escuela	demux	fundamentals
story of project	transistor animated (utube)	NGC4697 bh mass
casa guides	sis mixer	phangs galaxy survey
vlbi	phase-lock loop (wiki)	large programs
science pipeline	lo1 optical fiber (memo 443)	vlbi m87 bh

# Questions?

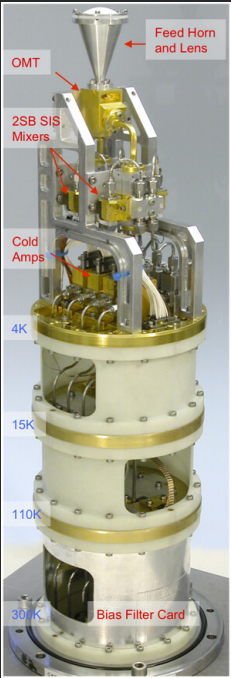
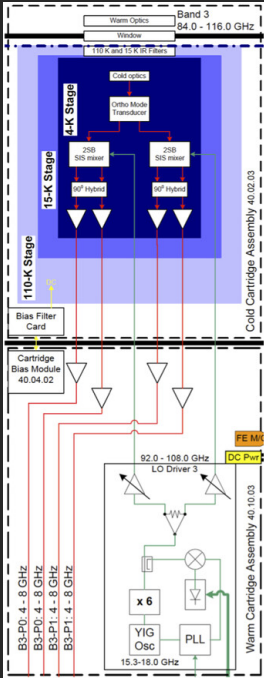


# Appendix

# Band List

N	Freq (GHz)	Wavelength (mm)	Country	Shape	Yig freq (GHz)	Warm mult	Cold mult
1	31.3 - 45	6.7 - 9.5	Taiwan/Chile	SSB	31.0 - 40.0	1	1
2	67 - 90	3.3 - 4.5	Europe/Chile	SSB	13.2 - 15.7	6	1
3	84 - 116	2.6 - 3.6	Canada	2SB	15.3 - 18.0	6	1
4	125 - 163	1.8 - 2.4	Japan	2SB	22.2 - 25.8	3	2
5	163 - 211	1.4 - 1.8	Sweden	2SB	13.8 - 16.9	6	2
6	211 - 275	1.1 - 1.4	USA	2SB	12.3 - 14.7	6	3
7	275 - 373	0.8 - 1.1	France	2SB	15.62 - 20.37	6	3
8	385 - 500	0.60 - 0.78	Japan	2SB	21.72 - 27.44	3	6
9	602 - 720	0.42 - 0.50	Netherlands	DSB	22.51 - 26.45	3	9
10	787 - 950	0.32 - 0.38	Japan	DSB	14.8 - 17.4	6	9

# Band 3 Diagram



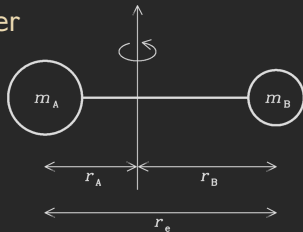
# Interstellar Molecules

2	3	4	5	6	7	8	9
H <sub>2</sub>	H <sub>2</sub> O	NH <sub>3</sub>	CH <sub>4</sub>	CH <sub>3</sub> OH	CH <sub>2</sub> CH(OH)	CH <sub>3</sub> COOH	(CH <sub>3</sub> ) <sub>2</sub> O
CO	H <sub>2</sub> S	H <sub>2</sub> CO(?)	SiH <sub>4</sub>	CH <sub>3</sub> SH	c-C <sub>2</sub> H <sub>4</sub> O	HC(O)OCH <sub>3</sub>	CH <sub>3</sub> CH <sub>2</sub> CN
CSi	HCN	H <sub>2</sub> CS	CH <sub>2</sub> NH	C <sub>2</sub> H <sub>4</sub>	HC(O)CH <sub>3</sub>	HOCH <sub>2</sub> C(O)H	CH <sub>3</sub> CH <sub>2</sub> OH
CP	HNC	C <sub>2</sub> H <sub>2</sub>	NH <sub>2</sub> CN	H(CC) <sub>2</sub> H	H <sub>3</sub> C-CC-H	H <sub>3</sub> C-CC-CN	CH <sub>3</sub> C <sub>4</sub> H
C <sub>5</sub>	CO <sub>2</sub>	HNCO	CH <sub>2</sub> CO	CH <sub>3</sub> CN	CH <sub>3</sub> NH <sub>2</sub>	H <sub>2</sub> C <sub>6</sub>	HCC-CG-CC-CN
NO	SO <sub>2</sub>	HNCS	HCOOH(?)	CH <sub>3</sub> NC	CH <sub>2</sub> CH(CN)	H(C <sub>2</sub> ) <sub>3</sub> H	C <sub>8</sub> H
N <sub>5</sub>	MgCN	H <sub>3</sub> O <sup>+</sup>	HCC-CN	HC(O)NH <sub>2</sub>	HCC-CG-CN	H <sub>2</sub> C=CH-C(O)H	CH <sub>3</sub> C(O)NH <sub>2</sub>
SO	MgNC	SiC <sub>3</sub>	HCC-NC	HCC-C(O)H	C <sub>6</sub> H	CH <sub>2</sub> CCHCN	C <sub>8</sub> H-
HCl	NaCN	C <sub>3</sub> S	c-C <sub>3</sub> H <sub>2</sub>	HC <sub>3</sub> NH <sup>+</sup>	C <sub>6</sub> H-	C <sub>7</sub> H	CH <sub>3</sub> CHCH <sub>2</sub>
NaCl	N <sub>2</sub> O	H <sub>2</sub> CN	l-C <sub>3</sub> H <sub>2</sub>	HC <sub>4</sub> N	H <sub>2</sub> NCH <sub>2</sub> CN		
KCl	NH <sub>2</sub>	c-C <sub>3</sub> H	CH <sub>2</sub> CN	C <sub>5</sub> N			
AlCl	OC <sub>5</sub>	l-C <sub>3</sub> H	H <sub>2</sub> COH <sup>+</sup>	C <sub>5</sub> H			
AlF	CH <sub>2</sub>	HCCN	C <sub>4</sub> Si	H <sub>2</sub> C <sub>4</sub>			
PN	HCO	CH <sub>3</sub>	C <sub>5</sub>	H <sub>2</sub> CCNH			
SiN	C <sub>3</sub>	C <sub>2</sub> CN	HNCCC	C <sub>5</sub> N-			
SiO	C <sub>2</sub> H	C <sub>3</sub> O	C <sub>4</sub> H	c-H <sub>2</sub> C <sub>3</sub> O			
SiS	C <sub>2</sub> O	HCNH <sup>+</sup>	C <sub>4</sub> H-				
NH	C <sub>2</sub> S	HOCO <sup>+</sup>	HC(O)CN				
OH	AlNC	CO <sub>2</sub>					
C <sub>2</sub>	HNO	C <sub>3</sub> N-					
CN	SiCN	HCNO					
HF	N <sub>2</sub> H <sup>+</sup>	HSCN					
FeO	SiNC	H <sub>2</sub> O <sub>2</sub>					
LiH	c-SiC <sub>2</sub>						
CH	HOC <sup>+</sup>						
CH <sup>+</sup>	HOC <sup>+</sup>						
CO <sup>+</sup>	HCS <sup>+</sup>						
SO <sup>+</sup>	H <sub>3</sub> <sup>+</sup>						
SH	OCN-						
O <sub>2</sub>	HCP						
N <sub>2</sub>	CCP						
				10	11	12	13
				(CH <sub>3</sub> ) <sub>2</sub> CO	HCC-CG-CG-CG-CN	C <sub>6</sub> H <sub>6</sub>	HCC-CG-CG-CG-CG-CN
				HOCH <sub>2</sub> CH <sub>2</sub> OH	CH <sub>3</sub> C <sub>6</sub> H	CH <sub>3</sub> CH <sub>2</sub> CH <sub>2</sub> CN	
				CH <sub>3</sub> OCH <sub>2</sub> OH	HC(O)OCH <sub>2</sub> CH <sub>3</sub>		
				H <sub>3</sub> C-CH <sub>2</sub> -C(O)H			
				CH <sub>3</sub> (CC) <sub>2</sub> CN			

# CO Emission Lines

$$\nu(J \rightarrow J-1) = \frac{hJ}{4\pi^2 m r_e^2}$$

Frequency      mass      diameter  
Orbital number



Because the rotational energy is:

$$E_{rot} = \frac{h}{2\pi I} J(J+1)$$

Where  $I$  is the inertial moment is:

$$I = m_A r_A^2 + m_B r_B^2$$

So the difference between 2 levels is:

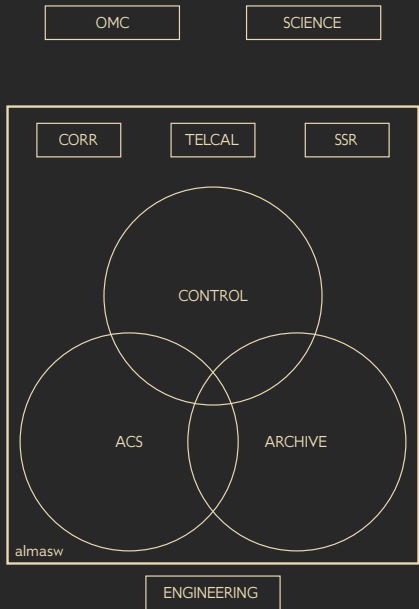
$$\Delta E_{rot}(J \rightarrow J-1) = [J(J+1) - (J-1)J] \frac{h^2}{2I} = \frac{h^2 J}{I}$$

Converting to frequency with another Planck constant gives:

$$\nu = \frac{\Delta E_{rot}}{h} = \frac{hJ}{2\pi I}$$

 $^{12}\text{C}^{16}\text{O}$ 

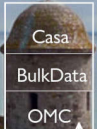

# Software Trinity







Continuous integration



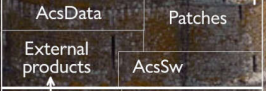
AlmaSw



Subsystems



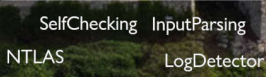
ACS



Build



Underworld



Meta